

## Sixth Semester B.E. Degree Examination, December 2012 Operations Research

Time: 3 hrs. Max. Marks:100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

## PART - A

- 1 a. What is operations research? Mention six phases of an operations research study. (06 Marks)
  - b. Old hens can be bought at Rs.50/- each but young ones cost Rs.100/- each. The old hens lay 3 eggs/week and young hens 5 eggs/week. Each egg cost Rs.2/- A hen costs Rs.5/- per week to feed. If a person has only Rs.2000/- to spend for hens, formulate the problem to decide how many of each kind of hen should he buy? Assume that he cannot house more than 40 hens
  - c. Solve the following L.P.P. graphically,

Maximize  $z = 100x_1 + 40x_2$ 

Subject to  $5x_1 + 2x_2 \le 1000$ 

$$3x_1 + 2x_2 \le 900$$

$$x_1 + 2x_2 \le 500$$
 and

$$x_1, x_2 \ge 0$$
 (07 Marks)

2 a. Mention five assumptions of linear programming.

(05 Marks)

b. Define and illustrate with examples slak variables and surplus variables.

(04 Marks)

c. Solve the following LPP:

Maximize 
$$z = 15x_1 + 6x_2 + 9x_3 + 2x_4$$

Subject to 
$$2x_1 + x_2 + 5x_3 + 6x_4 \le 20$$

$$3x_1 + x_2 + 3x_3 + 25x_4 \le 24$$

$$7x_1 + x_4 \le 70$$

$$x_1, x_2, x_3 \ge 0$$
 (11 Marks)

3 a. Explain two phase technique to solve LPP in simplex method.

(06 Marks)

b. Use Big-M method to solve the following LPP:

Minimize  $z = 4x_1 + 3x_2$ 

Subject to  $2x_1 + x_2 \ge 10$ 

$$-3x_1 + 2x_2 \le 6$$

$$x_1 + x_2 \ge 6$$

and  $x_1, x_2 \ge 0$ 

(14 Marks)

4 a. What are the important characteristics of duality?

(05 Marks)

b. Explain the conceptual procedure of revised simplex method in standard form.

4 c. Write the dual of the following LPP:

Minimize 
$$z = 3x_1 - 6x_2 + 4x_3$$
  
Subject to  $4x_1 + 3x_2 + 6x_3 \ge 9$   
 $x_1 + 2x_2 + 3x_3 \ge 6$   
 $6x_1 - 2x_2 - 2x_3 \le 10$   
 $x_1 - 2x_2 + 6x_3 \ge 4$   
 $2x_1 + 5x_2 - 3x_3 \ge 6$   
 $x_1, x_2, x_3 \ge 0$ 

(05 Marks)

## PART - B

5 a. Explain sensitivity analysis.

(08 Marks)

b. Use the dual simplex method to solve the following LPP:

Maximize 
$$z = -2x_1 - 2x_2 - 4x_3$$
  
Subject to  $2x_1 + 3x_2 + 5x_3 \ge 2$   
 $3x_1 + x_2 + 7x_3 \le 3$   
 $x_1 + 4x_2 + 6x_3 \le 5$   
and  $x_1, x_2, x_3 \ge 0$ 

(12 Marks)

6 a. Explain different steps in Hungarian algorithm to solve an assignment problem. (08 Marks)

b. Find the optimal transportation cost of the following matrix by using least cost method.

(12 Marks)

	Α	В	С	D	E	Supply
P	4	1	2	6	9	100
Q	6	4	3	5	7	120
R	5	2	6	4	8	120
Demand	40	50	70	90	90	

7 a. Solve the game whose pay off matrix is given by,

(08 Marks)

- b. Explain the following:
  - i) Minimax and maximin principles.
  - ii) Pure and mixed strategies.
  - iii) Two person zero sum game.
  - iv) Dominance principles.

(12 Marks)

(05 Marks)

- 8 a. Give a note on basic simulated annealing algorithm. (05 Marks)
  - b. Write an outline of a basic genetic algorithm.
  - c. Explain table search algorithm. (05 Marks)
  - d. Explain decision trees. (05 Marks)